

Evidence for the $\eta_b(2S)$ and observation of $h_b(1P) \rightarrow \eta_b(1S)\gamma$ and $h_b(2P) \rightarrow \eta_b(1S)\gamma$

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(Dated: 20 July 2012)

We report the first evidence for the $\eta_b(2S)$ using the $h_b(2P) \rightarrow \eta_b(2S)\gamma$ transition and the first observation of the $h_b(1P) \rightarrow \eta_b(1S)\gamma$ and $h_b(2P) \rightarrow \eta_b(1S)\gamma$ transitions. The mass and width of the $\eta_b(1S)$ and $\eta_b(2S)$ are measured to be $m_{\eta_b(1S)} = (9402.4 \pm 1.5 \pm 1.8) \text{ MeV}/c^2$, $m_{\eta_b(2S)} = (9999.0 \pm 3.5^{+2.8}_{-1.9}) \text{ MeV}/c^2$ and $\Gamma_{\eta_b(1S)} = (10.8^{+4.0}_{-3.7}{}^{+4.5}_{-2.0}) \text{ MeV}$. We also update the $h_b(1P)$ and $h_b(2P)$ mass measurements. We use a 133.4 fb^{-1} data sample collected at energies near the $\Upsilon(5S)$ resonance with the Belle detector at the KEKB asymmetric-energy e^+e^- collider.

PACS numbers: 14.40.Pq, 13.25.Gv, 12.39.Pn

Bottomonium, a bound system of a $b\bar{b}$ quark-antiquark pair, is well described by nonrelativistic quantum mechanics due to the slow motion of the heavy quarks [1]. The spin-singlet ($S = 0$) states of the quark pair with zero orbital momentum, $L = 0$, are customarily called $\eta_b(nS)$ with $n = 1, 2, \dots$. The hyperfine splitting ΔM_{HF} from the corresponding spin-triplet state, *i.e.* the mass difference between the $\Upsilon(nS)$ and $\eta_b(nS)$, provides an important measure of the spin-spin interaction between the quark and the antiquark. The existing measurements [2] of the $\eta_b(1S)$ mass are only in marginal agreement with theoretical expectations [3, 4] and the $\eta_b(1S)$ width is yet to be measured. There is no information available on the radially excited state $\eta_b(2S)$.

In this Letter, we report the first evidence for the $\eta_b(2S)$ in the $h_b(2P) \rightarrow \eta_b(2S)\gamma$ transition and the first observation of the $h_b(1P) \rightarrow \eta_b(1S)\gamma$ and $h_b(2P) \rightarrow \eta_b(1S)\gamma$ transitions. We use a 121.4 fb^{-1} data sample at the $\Upsilon(5S)$ resonance and 12.0 fb^{-1} of energy-scan data collected nearby with the Belle detector [5] at the KEKB asymmetric-energy e^+e^- collider [6].

We study the processes $e^+e^- \rightarrow \Upsilon(5S) \rightarrow h_b(nP)\pi^+\pi^- \rightarrow [\eta_b(mS)\gamma]\pi^+\pi^-$ in which the $\eta_b(mS)$

states are reconstructed inclusively. The approximate values of the expected energies of the photons in the $h_b(nP)$ rest frame are given in Table I. The $h_b(nP)$ signal is tagged using the missing mass of the $\pi^+\pi^-$ pair $M_{\text{miss}}(\pi^+\pi^-)$, while the $\eta_b(mS)$ signal is tagged using the variable $M_{\text{miss}}^{(n)}(\pi^+\pi^-\gamma) \equiv M_{\text{miss}}(\pi^+\pi^-\gamma) - M_{\text{miss}}(\pi^+\pi^-) + m_{h_b(nP)}$. The missing mass is defined via $M_{\text{miss}}(X) = \sqrt{(E_{\text{c.m.}} - E_X^*)^2 - p_X^{*2}}$, where $E_{\text{c.m.}}$ is the center-of-mass (c.m.) energy and E_X^* and p_X^* are the energy and momentum of the system X measured in the c.m. frame. We fit the $M_{\text{miss}}(\pi^+\pi^-)$ spectra for different $M_{\text{miss}}^{(n)}(\pi^+\pi^-\gamma)$ bins to measure the $h_b(nP)$ yield. This procedure removes the background due to random $\pi^+\pi^-$ combinations. The $h_b(nP)$ yield peaks at $M_{\text{miss}}^{(n)}(\pi^+\pi^-\gamma)$ values corresponding to the masses of the $\eta_b(mS)$ states from the $h_b(nP) \rightarrow \eta_b(mS)\gamma$ transitions.

The selection criteria for the $\pi^+\pi^-$ pairs are the same as those described in Ref. [7]. We use events that pass the Belle-standard hadronic event selection and consider all positively identified $\pi^+\pi^-$ pairs that originate from the vicinity of the interaction point. Belle previously observed that the decay $\Upsilon(5S) \rightarrow h_b(nP)\pi^+\pi^-$ pro-

TABLE I: Expected photon energies in $h_b(nP) \rightarrow \eta_b(mS)\gamma$ transitions (E_γ), π^0 veto parameters (ΔM and E_{th}) and the parameter σ of the $M_{\text{miss}}^{(n)}(\pi^+\pi^-\gamma)$ resolution function.

	E_γ , MeV	ΔM , MeV/ c^2	E_{th} , MeV	σ , MeV/ c^2
$h_b(2P) \rightarrow \eta_b(2S)\gamma$	260	10	125	13.6 ± 1.1
$h_b(1P) \rightarrow \eta_b(1S)\gamma$	500	13	75	19.8 ± 1.1
$h_b(2P) \rightarrow \eta_b(1S)\gamma$	860	17	75	8.6 ± 0.7

ceeds via the intermediate resonances $Z_b(10610)$ and $Z_b(10650)$ [8]. We exploit this with the additional requirement $10.59 \text{ GeV}/c^2 < M_{\text{miss}}(\pi^\pm) < 10.67 \text{ GeV}/c^2$, which suppresses the combinatorial background by a factor of 5 [1.6] for the $h_b(1P)$ [$h_b(2P)$] without any significant loss of the signal. Photon candidates are clusters in the electromagnetic calorimeter that are not associated with charged tracks. We apply a veto on $\pi^0 \rightarrow \gamma\gamma$ decays, rejecting a photon candidate if the invariant mass of it and any other photon in the event with energy above the threshold E_{th} is within ΔM of the π^0 mass. The parameters E_{th} and ΔM , listed in Table I, are chosen by maximizing the ratio $\frac{S}{\sqrt{B}}$, where S is the number of signal events in the Monte Carlo (MC) simulation and B is the number of background events estimated from a small fraction (0.1%) of the data. To suppress continuum $e^+e^- \rightarrow q\bar{q}$ ($q = u, d, s, c$) background, we use the ratio R_2 of the second- to zeroth-order Fox-Wolfram moments [9]. In the $\eta_b(1S)$ analysis, we require $R_2 < 0.3$, which was optimized using the $\Upsilon(5S) \rightarrow \Upsilon(2S)\pi^+\pi^-$ decays [7]. For the high statistics $h_b(1P) \rightarrow \eta_b(1S)\gamma$ transition, the optimum is shifted to $R_2 < 0.32$, which we adopt here for the $\eta_b(2S)$ analysis.

To calibrate the photon energy resolution function, we use three control channels: $D^{*0} \rightarrow \gamma D^0 (\rightarrow K^-\pi^+)$, $\pi^0 \rightarrow \gamma\gamma$ and $\eta \rightarrow \gamma\gamma$. For the two-photon final states, we require that the energies of the photons in the laboratory frame be almost equal: $|E_1 - E_2|/(E_1 + E_2) < 0.05$. This reduces the resolution shape dependence to a single variable. The resolution shape is parameterized by a double-sided bifurcated Crystal Ball function [10] in which a bifurcated Gaussian is smoothly joined with power law tails on both sides. The signal is extracted using the $M(K^-\pi^+\gamma) - M(K^-\pi^+) + m_{D^0}$ distribution for the D^{*0} and $M(\gamma\gamma)$ for the π^0 and η . From comparisons of the peak positions and widths in data and MC simulation, we determine shifts in the photon energy $\Delta E/E$ and width correction factors f as a function of E . Various calibration channels give consistent results; an uncertainty is assigned based on their spread. These translate to typical mass shift and width-correction factors of $1.2 \text{ MeV}/c^2$ and 1.13 , respectively. Average values of left and right widths (σ) of the bifurcated Gaussian components of the $M_{\text{miss}}^{(n)}(\pi^+\pi^-\gamma)$ resolution functions are given in Table I.

We update previous Belle measurements of the $h_b(nP)$ masses [7], incorporating a 10% increase in statistics and the requirement of an intermediate Z_b [11]. The results of the fits are shown in Figs 1 and 2 and the fitted signal parameters are listed in Table II. The confidence level of

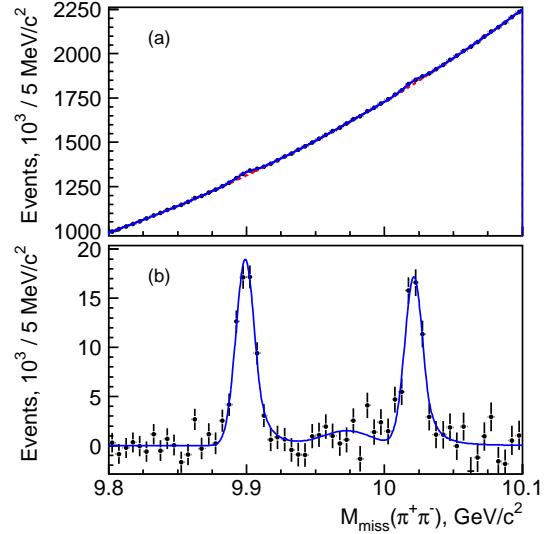


FIG. 1: (colored online) The $M_{\text{miss}}(\pi^+\pi^-)$ spectrum in the $h_b(1P)$ region. In (a) the data are the points with error bars with the fit function (blue solid curve) and background (red dashed curve) overlaid. (b) shows the background subtracted data (points with error bars) while the signal component of the fit is overlaid (blue curve). The background is combinatorial.

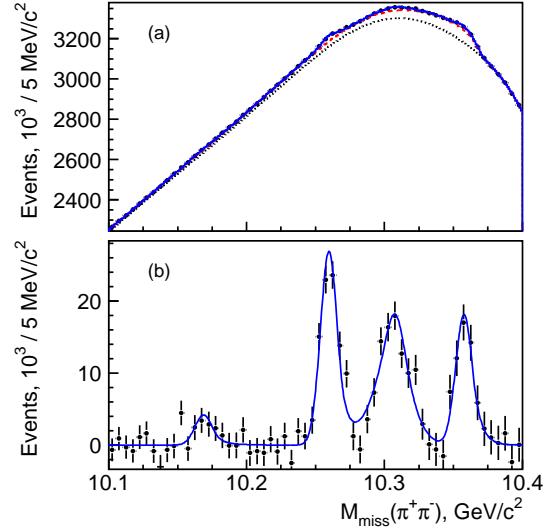


FIG. 2: (colored online) The $M_{\text{miss}}(\pi^+\pi^-)$ spectrum in the $h_b(2P)$ region. The legend is the same as in Fig. 1. The background components are random combinations and $K_S^0 \rightarrow \pi^+\pi^-$ decays. The combinatorial component is shown in (a) by the black dotted curve.

the fit in the $h_b(1P)$ [$h_b(2P)$] region is 35% [70%]. The es-

TABLE II: The yield and mass of peaking components from the fits to the $M_{\text{miss}}(\pi^+\pi^-)$. Here and everywhere in this Letter, the first quoted uncertainty is statistical (unless stated otherwise) and the second (if present) is systematic.

	$N, 10^3$	Mass, MeV/c^2
$\Upsilon(5S) \rightarrow h_b(1P)$	$70.3 \pm 3.3^{+1.9}_{-0.7}$	$9899.1 \pm 0.4 \pm 1.0$
$\Upsilon(3S) \rightarrow \Upsilon(1S)$	13 ± 7	9973.0
$\Upsilon(5S) \rightarrow \Upsilon(2S)$	61.3 ± 4.1	10021.3 ± 0.5
$\Upsilon(5S) \rightarrow \Upsilon(1D)$	14 ± 7	10169 ± 3
$\Upsilon(5S) \rightarrow h_b(2P)$	$89.5 \pm 6.1^{+0.0}_{-5.8}$	$10259.8 \pm 0.5 \pm 1.1$
$\Upsilon(2S) \rightarrow \Upsilon(1S)$	97 ± 12	10305.6 ± 1.2
$\Upsilon(5S) \rightarrow \Upsilon(3S)$	58 ± 8	10357.7 ± 1.0

timation of systematic uncertainties follows Ref. [7]. For hyperfine splittings $\sum_{J=0}^2 \frac{2J+1}{9} m_{\chi_{bJ}(nP)} - m_{h_b(nP)}$, we find $\Delta M_{\text{HF}}(1P) = (+0.8 \pm 1.1) \text{ MeV}/c^2$ and $\Delta M_{\text{HF}}(2P) = (+0.5 \pm 1.2) \text{ MeV}/c^2$, where statistical and systematic uncertainties in mass are added in quadrature.

We fit the $M_{\text{miss}}(\pi^+\pi^-)$ spectra for each $M_{\text{miss}}^{(n)}(\pi^+\pi^-\gamma)$ bin to measure the $h_b(nP)$ yield as a function of $M_{\text{miss}}^{(n)}(\pi^+\pi^-\gamma)$. We fix the masses of the peaking components at the values given in Table II. Although the $M_{\text{miss}}(\pi^+\pi^-)$ combinatorial background shape in the $h_b(2P)$ region is rather complicated (described by an eighth-order Chebyshev polynomial), it changes slowly with $M_{\text{miss}}^{(2)}(\pi^+\pi^-\gamma)$. For the $M_{\text{miss}}(\pi^+\pi^-)$ fits for each bin, we multiply the polynomial shape with parameters fixed at their values from the overall fit by a lower-order polynomial with floating coefficients; this procedure improves the accuracy of the $h_b(nP)$ yield measurements. For this lower-order function, we use a first- [fifth-] order polynomial for the $\eta_b(1S)$ [$\eta_b(2S)$] $M_{\text{miss}}^{(2)}(\pi^+\pi^-\gamma)$ region. From a generic MC simulation, we find that the $K_S^0 \rightarrow \pi^+\pi^-$ contribution is independent of the $M_{\text{miss}}^{(2)}(\pi^+\pi^-\gamma)$ value in the $\eta_b(1S)$ region; in the $\eta_b(2S)$ region, we restrict the $M_{\text{miss}}(\pi^+\pi^-)$ fit range to $10.10 \text{ GeV}/c^2 - 10.34 \text{ GeV}/c^2$, thereby avoiding the sharp rise in the $K_S^0 \rightarrow \pi^+\pi^-$ contribution that occurs at $10.37 \text{ GeV}/c^2$. The results for the $h_b(1P)$ and $h_b(2P)$ yields as a function of $M_{\text{miss}}^{(n)}(\pi^+\pi^-\gamma)$ are presented in Fig. 3. Clear peaks at $9.4 \text{ GeV}/c^2$ and $10.0 \text{ GeV}/c^2$ are identified as signals for the $\eta_b(1S)$ and $\eta_b(2S)$, respectively. Generic MC simulations indicate that no peaking backgrounds are expected in these spectra.

We fit the $h_b(nP)$ yield dependence on $M_{\text{miss}}^{(n)}(\pi^+\pi^-\gamma)$ to a sum of the $\eta_b(nS)$ signal components described by the convolution of a non-relativistic Breit-Wigner function with the calibrated resolution function described above and a background parameterized by an exponentiation of a first- [second-] order polynomial in the $\eta_b(1S)$

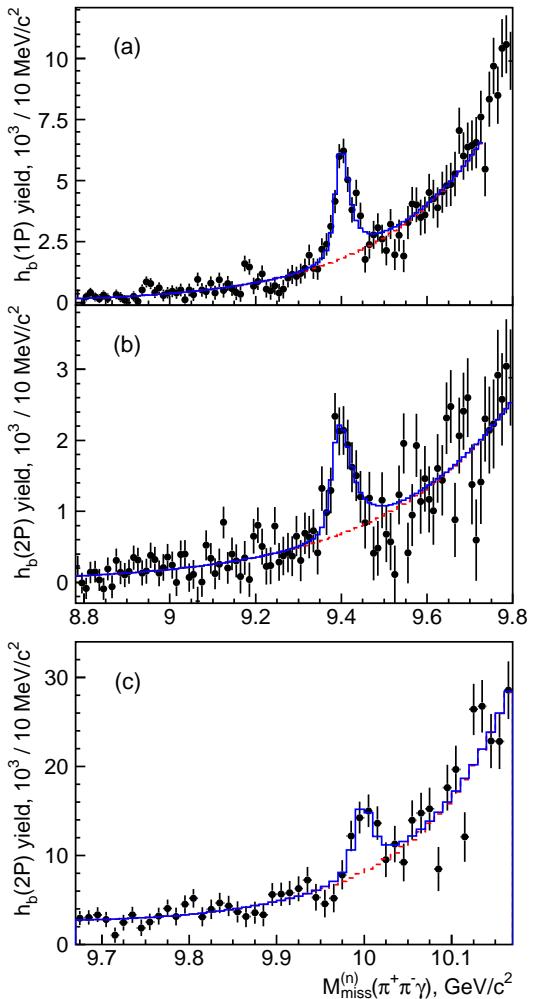


FIG. 3: The $h_b(1P)$ yield vs. $M_{\text{miss}}^{(1)}(\pi^+\pi^-\gamma)$ (a), and $h_b(2P)$ yield vs. $M_{\text{miss}}^{(2)}(\pi^+\pi^-\gamma)$ in the $\eta_b(1S)$ region (b) and in the $\eta_b(2S)$ region (c). The solid (dashed) histogram is the fit result (background component of the fit function).

[$\eta_b(2S)$] region. The two $M_{\text{miss}}^{(n)}(\pi^+\pi^-\gamma)$ spectra [from the $h_b(1P)$ and $h_b(2P)$] with $\eta_b(1S)$ signals are fitted simultaneously. We take into account the effect of multiple photons in the same $M_{\text{miss}}^{(n)}(\pi^+\pi^-\gamma)$ bin by increasing the errors in the corresponding $M_{\text{miss}}(\pi^+\pi^-)$ histogram. We find event yields for the $h_b(nP) \rightarrow \eta_b(mS)$ transitions of $N_{1P \rightarrow 1S} = (23.5 \pm 2.0) \times 10^3$, $N_{2P \rightarrow 1S} = (10.3 \pm 1.3) \times 10^3$ and $N_{2P \rightarrow 2S} = (25.8 \pm 4.9) \times 10^3$; the fitted masses and width are $m_{\eta_b(1S)} = (9402.4 \pm 1.5 \pm 1.8) \text{ MeV}/c^2$, $\Gamma_{\eta_b(1S)} = (10.8^{+4.0}_{-3.7}{}^{+4.5}_{-2.0}) \text{ MeV}$ and $m_{\eta_b(2S)} = (9999.0 \pm 3.5^{+2.8}_{-1.9}) \text{ MeV}/c^2$. The confidence level of the $\eta_b(1S)$ [$\eta_b(2S)$] fit is 61% [36%]. If the $\eta_b(2S)$ width is allowed to float in the fit, we find $\Gamma_{\eta_b(2S)} = (4^{+12}_{-20}) \text{ MeV}$ or $\Gamma_{\eta_b(2S)} < 24 \text{ MeV}$ at 90% C.L. using the Feldman-Cousins approach [12]. For the $\eta_b(2S)$ mass determination and yield measurements quoted above, we fix the $\eta_b(2S)$ width at its value from perturbative calcula-

tions [13] $\Gamma_{\eta_b(2S)} = \Gamma_{\eta_b(1S)} \frac{\Gamma_{ee}^{\Upsilon(2S)}}{\Gamma_{ee}^{\Upsilon(1S)}}$ = $(4.9^{+2.7}_{-1.9})$ MeV, where the uncertainty is due to our experimental uncertainty in $\Gamma_{\eta_b(1S)}$.

To estimate the systematic uncertainties in the $\eta_b(nS)$ parameters, we vary the polynomial orders and fit intervals in the $M_{\text{miss}}(\pi^+\pi^-)$ & $M_{\text{miss}}^{(n)}(\pi^+\pi^-\gamma)$ fits, and the $M_{\text{miss}}^{(n)}(\pi^+\pi^-\gamma)$ binning by scanning the starting point of the $10 \text{ MeV}/c^2$ bin with $1 \text{ MeV}/c^2$ steps. We also multiply the non-relativistic Breit-Wigner function by an E_γ^3 term expected for an electric dipole transition and include the uncertainty in the $h_b(1P)$ and $h_b(2P)$ masses and in the estimated value of the $\eta_b(2S)$ width. The contribution of each source is given in Table III. We add the various contributions in quadrature to estimate the total systematic uncertainty. We repeat the analysis using signal MC simulation instead of data and find no shift of the $\eta_b(nS)$ parameters compared to the MC input. For the hyperfine splittings $m_{\Upsilon(nS)} - m_{\eta_b(nS)}$ we determine $\Delta M_{\text{HF}}(1S) = (57.9 \pm 2.3) \text{ MeV}/c^2$ and $\Delta M_{\text{HF}}(2S) = (24.3^{+4.0}_{-4.5}) \text{ MeV}/c^2$, where statistical and systematic uncertainties in mass are added in quadrature.

TABLE III: Systematic uncertainties in the $\eta_b(1S)$ and $\eta_b(2S)$ masses (in MeV/c^2) and in the $\eta_b(1S)$ width (in MeV).

	$m_{\eta_b(1S)}$	$\Gamma_{\eta_b(1S)}$	$m_{\eta_b(2S)}$
$M_{\text{miss}}(\pi^+\pi^-)$ fits	+0.1 -0.2	+0.0 -0.8	+0.0 -0.1
$M_{\text{miss}}^{(n)}(\pi^+\pi^-\gamma)$ binning	+0.2 -0.5	+0.7 -0.8	+2.3 -1.4
$M_{\text{miss}}^{(n)}(\pi^+\pi^-\gamma)$ fit	+0.2 -0.0	+4.2 -0.6	+0.5 -0.2
Calibration	± 1.4	± 1.5	± 0.7
$\eta_b(nS)$ line shape	+0.6 -0.0	+0.0 -0.4	+0.6 -0.0
$h_b(nP)$ mass	± 0.9	± 0.0	± 1.1
$\eta_b(2S)$ width	-	-	+0.1 -0.0
Total	± 1.8	+4.5 -2.0	+2.8 -1.9

Using Wilks' theorem [15], we find 15σ [9σ] for the $h_b(1P) \rightarrow \eta_b(1S)\gamma$ [$h_b(2P) \rightarrow \eta_b(1S)\gamma$] statistical significance. For the significance of the $\eta_b(2S)$ signal, we use a method that takes into account the trial factor associated with the definition of the search window or the so-called “look-elsewhere effect” [16]. To determine this window, we conservatively assume $r = 0$ and $r = 1$ for the ratio $r = \frac{\Delta M_{\text{HF}}(2S)}{\Delta M_{\text{HF}}(1S)}$. (For reference, the measured value of $r = 0.420^{+0.071}_{-0.079}$ is consistent with perturbative calculations [14] that predict $\frac{m_{\Upsilon(2S)}^2}{m_{\Upsilon(1S)}^2} \frac{\Gamma_{ee}^{\Upsilon(2S)}}{\Gamma_{ee}^{\Upsilon(1S)}} = 0.513 \pm 0.011$, where the error is due to the uncertainties in Γ_{ee} .) We find the significance of the $\eta_b(2S)$ signal to be 4.8σ (4.2σ including systematics).

Branching fractions $\mathcal{B}[h_b(nP) \rightarrow \eta_b(mS)\gamma]$ are determined from $N_{nP \rightarrow mS}^{\text{total}} / (N_{nP}^{\text{total}} \epsilon)$, where $N_{nP \rightarrow mS}^{\text{total}} = N_{nP \rightarrow mS} + N_{nP \rightarrow mS}^{\text{anti-cut}}$ and $N_{nP}^{\text{total}} = N_{nP} + N_{nP}^{\text{anti-cut}}$,

$N_{nP \rightarrow mS}^{\text{anti-cut}}$ [$N_{nP}^{\text{anti-cut}}$] is the number of the $h_b(nP) \rightarrow \eta_b(mS)\gamma$ transitions [$h_b(nP)$] that are rejected by the R_2 and π^0 veto requirements [by the R_2 requirement], ϵ is the reconstruction efficiency of the photon. In this way, we do not rely on MC simulation for the determination of the efficiency of the R_2 and π^0 veto requirements. To determine $N_{nP}^{\text{anti-cut}}$ and $N_{nP \rightarrow mS}^{\text{anti-cut}}$, we repeat the analysis for the events rejected by the corresponding requirements. In the $M_{\text{miss}}^{(n)}(\pi^+\pi^-\gamma)$ [$M_{\text{miss}}(\pi^+\pi^-)$] fits, we fix the $\eta_b(mS)$ mass and width [the $h_b(nP)$ mass]. We estimate the $N_{nP}^{\text{anti-cut}}$ systematic uncertainty by varying the polynomial order and fit range in the $M_{\text{miss}}(\pi^+\pi^-)$ fit and by varying the $h_b(nP)$ mass within its uncertainty. We find $N_{1P}^{\text{total}} = (84.2 \pm 4.4^{+2.1}_{-1.3}) \times 10^3$ and $N_{2P}^{\text{total}} = (98.5 \pm 8.1^{+5.5}_{-6.3}) \times 10^3$. For N^{total} , we add the N and $N^{\text{anti-cut}}$ uncertainties in quadrature. The contributions from the various sources of systematic uncertainty to the $N_{nP \rightarrow mS}^{\text{total}}$ are given in Table IV. The $h_b(nP)$ signal shape uncertainty is not considered for the yields, since it cancels in the ratio $N_{nP \rightarrow mS}^{\text{total}} / N_{nP}^{\text{total}}$. In combining the $N_{nP \rightarrow mS}$ and $N_{nP \rightarrow mS}^{\text{anti-cut}}$ uncertainties, we take into account correlations of the calibration and $\eta_b(nS)$ line shape sources. We find $N_{1P \rightarrow 1S}^{\text{total}} = (30.9 \pm 3.2^{+3.4}_{-1.8}) \times 10^3$, $N_{2P \rightarrow 1S}^{\text{total}} = (16.1 \pm 2.4^{+2.0}_{-2.2}) \times 10^3$ and $N_{2P \rightarrow 2S}^{\text{total}} = (35.6 \pm 7.3^{+4.5}_{-5.4}) \times 10^3$.

TABLE IV: Systematic uncertainties in the total yields of the $h_b(1P) \rightarrow \eta_b(1S)\gamma$, $h_b(2P) \rightarrow \eta_b(1S)\gamma$ and $h_b(2P) \rightarrow \eta_b(2S)\gamma$ transitions (in 10^3).

	$N_{1P \rightarrow 1S}^{\text{total}}$	$N_{2P \rightarrow 1S}^{\text{total}}$	$N_{2P \rightarrow 2S}^{\text{total}}$
$M_{\text{miss}}(\pi^+\pi^-)$ fits	+0.2 -1.1	+1.6 -1.8	+0.0 -1.3
$M_{\text{miss}}^{(n)}(\pi^+\pi^-\gamma)$ binning	+1.0 -0.3	+0.5 -0.1	+1.5 -3.7
$M_{\text{miss}}^{(n)}(\pi^+\pi^-\gamma)$ fit	+3.2 -1.2	+1.0 -1.3	+2.5 -2.1
Calibration	+0.3 -0.4	± 0.0	± 1.3
$\eta_b(nS)$ line shape	+0.2 -0.0	+0.1 -0.0	+0.3 -0.0
$\eta_b(nS)$ mass & width	+0.7 -0.5	± 0.3	+3.1 -2.8
Total	+3.4 -1.8	+2.0 -2.2	+4.5 -5.4

The efficiency is determined using phase-space MC simulated events that we weight according to the expectation $1 - \cos^2 \theta_\gamma + 2 \cos \theta_\gamma \cos \theta_{\pi^+} \cos \theta_{\pi^+\gamma}$ [17], where θ_γ (θ_{π^+}) is the angle between the beam axis and γ (π^+) momentum and $\theta_{\pi^+\gamma}$ is the angle between γ and π^+ momenta, with all momenta measured in the c.m. frame. Efficiencies to reconstruct the photon after the $\pi^+\pi^-$ pair is already reconstructed are 74.6% for $h_b(1P) \rightarrow \eta_b(1S)\gamma$, 73.4% for $h_b(2P) \rightarrow \eta_b(1S)\gamma$ and 76.1% for $h_b(2P) \rightarrow \eta_b(2S)\gamma$. The $\eta_b(1S)$ [$\eta_b(2S)$] signal function is normalized to unity in the mass window $9.3 \text{ GeV}/c^2 - 9.5 \text{ GeV}/c^2$ [$9.9 \text{ GeV}/c^2 - 10.1 \text{ GeV}/c^2$]; thus, the yields and efficiencies correspond to this mass window. The efficiencies have relative uncertainties of 2% due to pos-

sible differences between the data and MC simulation, and $^{+0.7\%}_{-0.8\%}$ [$^{+0.5\%}_{-0.6\%}$] due to the uncertainty in the $\eta_b(1S)$ [$\eta_b(2S)$] width. We find $\mathcal{B}[h_b(1P) \rightarrow \eta_b(1S)\gamma] = (49.2 \pm 5.7^{+5.6}_{-3.3}\%)$, $\mathcal{B}[h_b(2P) \rightarrow \eta_b(1S)\gamma] = (22.3 \pm 3.8^{+3.1}_{-3.3}\%)$ and $\mathcal{B}[h_b(2P) \rightarrow \eta_b(2S)\gamma] = (47.5 \pm 10.5^{+6.8}_{-7.7}\%)$. These branching fractions are a factor of 1.2 to 2.5 higher than theoretical expectations [18].

In summary, we report the first evidence for the $\eta_b(2S)$ using the $h_b(2P) \rightarrow \eta_b(2S)\gamma$ transition, with a significance, including systematics, of 4.2σ , and the first observation of the $h_b(1P) \rightarrow \eta_b(1S)\gamma$ and $h_b(2P) \rightarrow \eta_b(1S)\gamma$ transitions. The mass and width parameters of the $\eta_b(1S)$ and $\eta_b(2S)$ are measured to be $m_{\eta_b(1S)} = (9402.4 \pm 1.5 \pm 1.8) \text{ MeV}/c^2$, $m_{\eta_b(2S)} = (9999.0 \pm 3.5^{+2.8}_{-1.9}) \text{ MeV}/c^2$ and $\Gamma_{\eta_b(1S)} = (10.8^{+4.0}_{-3.7}{}^{+4.5}_{-2.0}) \text{ MeV}$. The $m_{\eta_b(2S)}$ and $\Gamma_{\eta_b(1S)}$ are first measurements; the $m_{\eta_b(1S)}$ measurement is more precise than the current world average and is $(11.4 \pm 3.6) \text{ MeV}/c^2$ above the central value [19]. The hyperfine splittings, $\Delta M_{\text{HF}}(1S) = (57.9 \pm 2.3) \text{ MeV}/c^2$, $\Delta M_{\text{HF}}(2S) = (24.3^{+4.0}_{-4.5}) \text{ MeV}/c^2$ and their ratio $0.420^{+0.071}_{-0.079}$, are in agreement with theoretical calculations [4, 20]. We update the $h_b(1P)$ and $h_b(2P)$ mass measurements $m_{h_b(1P)} = (9899.1 \pm 0.4 \pm 1.0) \text{ MeV}/c^2$, $m_{h_b(2P)} = (10259.8 \pm 0.5 \pm 1.1) \text{ MeV}/c^2$, and 1P and 2P hyperfine splittings $\Delta M_{\text{HF}}(1P) = (+0.8 \pm 1.1) \text{ MeV}/c^2$, $\Delta M_{\text{HF}}(2P) = (+0.5 \pm 1.2) \text{ MeV}/c^2$. These results supersede those in Ref. [7].

We are grateful to A. M. Badalian, Yu. S. Kalashnikova and M. B. Voloshin for useful discussions. We thank the KEKB group for excellent operation of the accelerator; the KEK cryogenics group for efficient solenoid operations; and the KEK computer group, the NII, and PNNL/EMSL for valuable computing and SINET4 network support. We acknowledge support from MEXT, JSPS and Nagoya's TLPSC (Japan); ARC and DIISR (Australia); NSFC (China); MSMT (Czechia); DST (India); INFN (Italy); MEST, NRF, GSDC of KISTI, and WCU (Korea); MNiSW (Poland); MES and RFIAAE (Russia); ARRS (Slovenia); SNSF (Switzerland); NSC and MOE (Taiwan); and DOE and NSF (USA).

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